

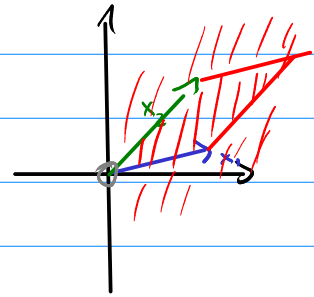
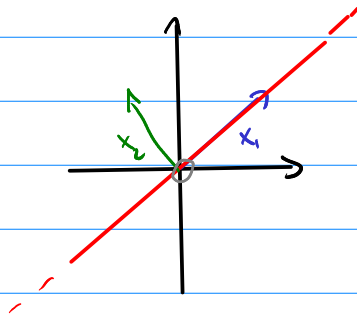
Vector space $x+y$ αx

Linear combination

$$\alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \dots + \alpha_n x_n$$

scalars vectors

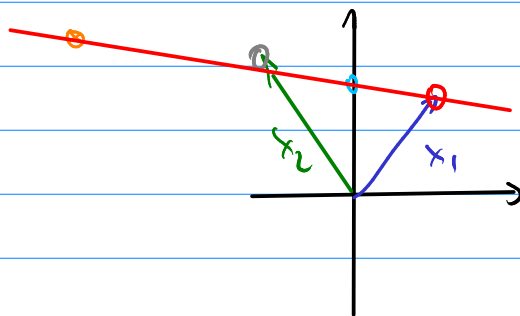
"coefficient"



Affine combination

$$\alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \dots + \alpha_n x_n$$

$$\alpha_1 + \dots + \alpha_n = 1$$



$$(\alpha_1, \alpha_2) = (1, 0)$$

$$(\alpha_1, \alpha_2) = (0, 1)$$

$$(\alpha_1, \alpha_2) = (0.5, 0.5)$$

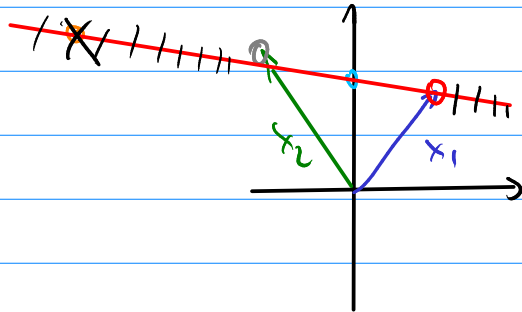
$$(\alpha_1, \alpha_2) = (-1, 2)$$

convex combination

$$\alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \dots + \alpha_n x_n$$

$$\alpha_1 + \dots + \alpha_n = 1$$

$$\alpha_1, \alpha_2, \dots, \alpha_n \geq 0$$



$$(\alpha_1, \alpha_2) = (1, 0)$$

$$(\alpha_1, \alpha_2) = (0, 1)$$

$$(\alpha_1, \alpha_2) = (0.5, 0.5)$$

$$\cancel{(\alpha_1, \alpha_2) = (-1, 2)}$$