Languages and Abstractions for High-Performance Scientific Computing CS598 APK

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Spring 2025

Introduction

Notes

Notes (unfilled, with empty boxes)

Notes (source code on Github)

About This Class

Why Bother with Parallel Computers?

Lowest Accessible Abstraction: Assembly

Architecture of an Execution Pipeline

Architecture of a Memory System

Shared-Memory Multiprocessors

Machine Abstractions

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Why this class?

| > | Setting: Performance-Constrained Code When is a code performance-constrained? |
|-------------|---|
| | |
| • | If your code is performance-constrained, what is the <i>best</i> approach? |
| | |
| • | If your code is performance-constrained, what is the <i>second-best</i> approach? |
| | |

Examples of Performance-Constrained Codes

Discussion:

- ▶ In what way are these codes constrained?
- ▶ How do these scale in terms of the problem size?

What Problem are we Trying To Solve?

$$(C_{ij})_{i,j=1}^{m,n} = \sum_{k=1}^{\ell} A_{ik} B_{kj}$$

- ► Reference BLAS DGEMM code
- ► OpenBLAS DGEMM code

Demo: intro/DGEMM Performance

Goals: What are we Allowed to Ask For?

- ► Goal: "make efficient use of the machine"
- In general: not an easy question to answer
- ▶ In theory: limited by *some* peak machine throughput
 - Memory Access
 - Compute
- ▶ In practice: many other limits (Instruction cache, TLB, memory hierarchy, NUMA, registers)

Class web page

https://bit.ly/hpcabstr-s25

contains:

- Class outline
- Slides/demos/materials
- Assignments
- Discussion Forum
- Grading Policies
- Video
- ► HW1 (soon)

Welcome Survey

Please go to:

https://bit.ly/hpcabstr-s25

and click on 'Start Activity'.

If you are seeing this later, you can find the activity at $\underline{\text{Activity:}}$ welcome-survey.

Grading / Workload

Four components:

- ► Homework: 25%
- ▶ Paper Presentation: 25%
 - ▶ 30 minutes (two per class)
 - Presentation sessions scheduled throughout the semester
 - Paper list on web page
 - Sign-up survey: soon
- ► Paper Reactions: 10%
- ► Computational Project: 40%

Open Source <3

These notes (and the accompanying demos) are open-source!

Bug reports and pull requests welcome:

https://github.com/inducer/hpc-lang-abstr-notes

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Approaches to High Performance

- ► Libraries (seen)
- ► Black-box Optimizing Compilers
- Compilers with Directives
- Code Transform Systems
- "Active Libraries"

Q: Give examples of the latter two.

Libraries: A Case Study

$$(C_{ij})_{i,j=1}^{m,n} = \sum_{k=1}^{\ell} A_{ik} B_{kj}$$

Demo: intro/DGEMM Performance

Do Libraries Stand a Chance? (in general)

► Tremendously successful approach — Name some examples

- ► Saw: Three simple integer parameters suffice to lose 'good' performance
 - ► Recent efforts: e.g. Batch BLAS
- Separation of Concerns

Example: Finite differences – e.g. implement ∂_x , ∂_y , ∂_z as separate (library) subroutines — What is the problem?

► Flexibility and composition

(Black-Box) Optimizing Compiler: Challenges

Why is black-box optimizing compilation so difficult?

- Application developer knowledge lost
 - ► Simple example: "Rough" matrix sizes
 - Data-dependent control flow
 - Data-dependent access patterns
 - Activities of other, possibly concurrent parts of the program
 - Profile-guided optimization can recover some knowledge
- ▶ Obtain proofs of required properties
- ➤ Size of the search space

 Consider http://polaris.cs.uiuc.edu/publications/padua.pdf

Directive-Based Compiler: Challenges

What is a directive-based compiler?

- Generally same as optimizing compiler
- Make use of extra promises made by the user
- ► What should the user promise?
- ▶ Ideally: feedback cycle between compiler and user
 - Often broken in both directions
 - User may not know what the compiler did
 - Compiler may not be able to express what it needs
- Directives: generally not mandatory

Lies, Lies Everywhere

- Semantics form a contract between programmer and language/environment
- ▶ Within those bounds, implementation has full freedom
- ► True at every level:
 - Assembly
 - ► "High-level" language (C)

Give examples of lies at these levels:



- "Domain-specific languages" ← A fresh language, I can do what I want!
- ► Consistent semantics are notoriously hard to develop
 - Especially as soon as you start allowing subsets of even (e.g.) C's

Class Outline

High-level Sections:

- ► Intro, Armchair-level Computer Architecture
- Machine Abstractions
- ▶ Performance: Expectation, Experiment, Observation
- Programming Languages for Performance
- Program Representation and Optimization Strategies
- Code Generation/JIT

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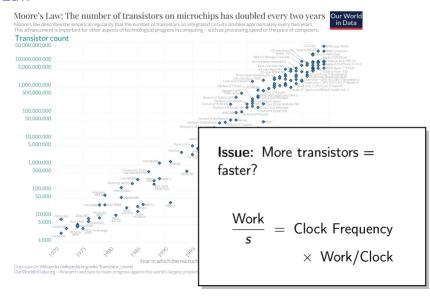
Architecture of an Execution Pipeline

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Shared-Memory Multiprocessors

Machine Abstractions

Moore's Law



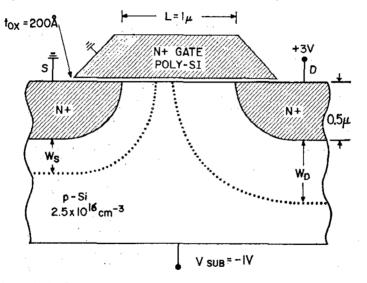
Dennard Scaling of MOSFETs

| Parameter | Factor |
|---------------------------|--------------|
| Dimension | $1/\kappa$ |
| Voltage | $1/\kappa$ |
| Current | $1/\kappa$ |
| Capacitance | $1/\kappa$ |
| Delay Time | $1/\kappa$ |
| Power dissipation/circuit | $1/\kappa^2$ |
| Power density | 1 |

[Dennard et al. '74, via Bohr '07]

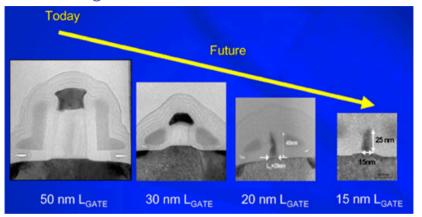
ightharpoonup Frequency = Delay time⁻¹

MOSFETs ("CMOS" – "complementary" MOS): Schematic



[Dennard et al. '74]

MOSFETs: Scaling



[Intel Corp.]

'New' problem at small scale:
 Sub-threshold leakage (due to low voltage, small structure)
 Dennard scaling is over – and has been for a while.

Peak Architectural Instructions per Clock: Intel

| CPU | IPC | Year |
|----------------------|-----|------|
| Pentium 1 | 1.1 | 1993 |
| Pentium 3 | 1.9 | 1999 |
| Pentium 4 (Gallatin) | 1.9 | 20 |
| Pentium D | 2 | 2005 |
| Pentium M | 2.5 | 2003 |
| Core 2 | 3 | 2006 |
| Sandy Bridge | <4 | 2011 |
| Skylake | <4 | 2015 |
| Golden Cove | <6 | 2021 |
| Lion Cove | <8 | 2024 |

[Charlie Brej http://brej.org/blog/?p=15, Wikipedia, Intel]

Context: Lemire: simdjson achieved IPC, '19 Discuss: How do we get out of this dilemma?

The Performance Dilemma

| IPC: Brick-ish WallClock Frequency: Brick Wall |
|---|
| Ideas: |
| |
| Question: What is the <i>conceptual</i> difference between those ideas? |
| |

The Performance Dilemma: Another Look

- Really: A crisis of the 'starts-at-the-top-ends-at-the-bottom' prorgramming model
- ► Tough luck: Most of our codes are written that way
- ► Even tougher luck: Everybody on the planet is *trained* to write codes this way

So:

▶ Need: Different tools/abstractions to write those codes

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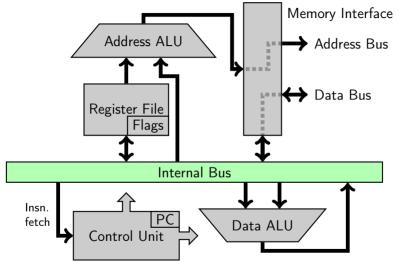
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Machine Abstractions

A Basic Processor: Closer to the Truth



- ▶ loosely based on Intel 8086
- ► What's a bus?

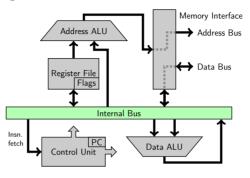
A Very Simple Program

```
c7 45 f4 05 00 00 00 mov1
                                                      $0x5,-0xc(%rbp)
int a = 5:
                                                      $0x11,-0x8(%rbp)
                           c7 45 f8 11 00 00 00 mov1
int b = 17:
                    12: 8b 45 f4
                                                      -0xc(%rbp),%eax
                                               mov
                                                      -0x8(\%rbp), \%eax
                   15: Of af 45 f8
                                               imul
int z = a * b:
                     19:
                          89 45 fc
                                                      %eax,-0x4(%rbp)
                                               mov
                           8b 45 fc
                                                      -0x4(\%rbp), \%eax
                     1c:
                                               mov
```

Things to know:

- Question: Which is it?
 - <opcode> <src>, <dest>
 - <opcode> <dest>, <src>
- Addressing modes (Immediate, Register, Base plus Offset)
- 0xHexadecimal

A Very Simple Program: Another Look



```
4:
         45 f4 05 00 00 00 movl
                                    $0x5.-0xc(%rbp)
b:
      c7 45 f8 11 00
                                    $0x11,-0x8(%rbp)
                      00
                         00
                            movl
12:
      8b 45 f4
                                    -0xc(%rbp),%eax
                            mov
15:
      Of af 45 f8
                                    -0x8(%rbp), %eax
                            imul
19:
      89 45 fc
                                    %eax,-0x4(%rbp)
                            mov
1c:
      8b 45 fc
                                    -0x4(\%rbp), %eax
                            mov
```

A Very Simple Program: Intel Form

```
4:
      c7 45 f4 05 00 00 00
                                       DWORD PTR [rbp-0xc],0x5
                               mov
      c7 45 f8 11 00 00 00
                                       DWORD PTR [rbp-0x8],0x11
h:
                               mov
12:
      8b 45 f4
                                       eax, DWORD PTR [rbp-0xc]
                               mov
                                       eax, DWORD PTR [rbp-0x8]
15:
    Of af 45 f8
                               imul
19: 89 45 fc
                                       DWORD PTR [rbp-0x4], eax
                               mov
1c:
      8b 45 fc
                                       eax, DWORD PTR [rbp-0x4]
                               mov
```

- "Intel Form": (you might see this on the net) <opcode> <sized dest>, <sized source>
- ► Previous: "AT&T Form": (we'll use this)
- ► Goal: Reading comprehension.
- ▶ Don't understand an opcode? https://en.wikipedia.org/wiki/X86_instruction_listings

Assembly Loops

```
55
                               0.
                                                             push
                                                                    %rbp
int main()
                                     48 89 65
                                                                    %rsp,%rbp
                                                             mov
                               4:
                                     c7 45 f8 00 00 00 00
                                                             Tvom
                                                                    $0x0.-0x8(%rbp)
                                     c7 45 fc 00 00 00 00
                               b:
                                                             movl
                                                                    $0x0,-0x4(%rbp)
   int y = 0, i;
                               12:
                                     eb 0a
                                                             qmp
                                                                    1e < main + 0x1e >
  for (i = 0;
                               14:
                                     8b 45 fc
                                                                    -0x4(\%rbp), %eax
                                                             mov
        y < 10; ++i
                               17:
                                     01 45 f8
                                                             add
                                                                    %eax,-0x8(%rbp)
                                     83 45 fc 01
                                                                    $0x1,-0x4(%rbp)
                               1a:
                                                             addl
     v += i:
                               1e:
                                     83 7d f8 09
                                                                    $0x9,-0x8(%rbp)
                                                             cmpl
                               22:
                                     7e f0
                                                             ile
                                                                    14 < main + 0x14 >
  return y;
                               24:
                                     8b 45 f8
                                                                    -0x8(%rbp),%eax
                                                             mov
                               27:
                                     c9
                                                             leaveg
                               28:
                                     с3
                                                             reta
```

Things to know:

- ► Condition Codes (Flags): Zero, Sign, Carry, etc.
- ► Call Stack: Stack frame, stack pointer, base pointer
- ► ABI: Calling conventions

Demos

Demo: intro/Assembly Reading Comprehension

```
Demo: Source-to-assembly mapping
Code to try:
int main()
{
   int y = 0, i;
   for (i = 0; y < 100; ++i)
      y += i*i;
   return y;
}</pre>
```

Also try https://godbolt.org for direct source-to-assembly mapping

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Performance: Expectation, Experiment, Observation

Modern Processors?

All of this can be built in about 4000 transistors. (e.g. MOS 6502 in Apple II, Commodore 64, Atari 2600)

So what exactly are Intel/ARM/AMD/Nvidia doing with the other billions of transistors?

Execution in a Simple Processor



- ► [IF] Instruction fetch
- ► [ID] Instruction Decode
- ► [EX] Execution
- ► [MEM] Memory Read/Write
- ► [WB] Result Writeback

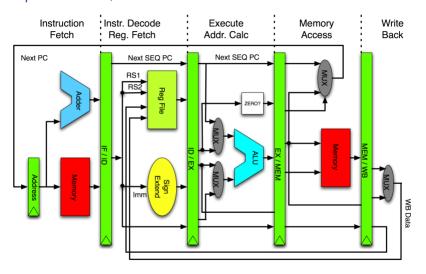
[Wikipedia @]

Solution: Pipelining



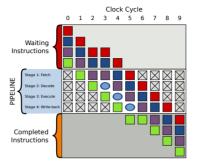
[Wikipedia @]

MIPS Pipeline: 110,000 transistors



[Wikipedia ©]

Hazards and Bubbles



Q: Types of Pipeline Hazards? (aka: what can go wrong?)

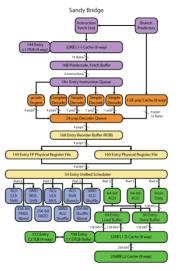


[Wikipedia @]

Demo

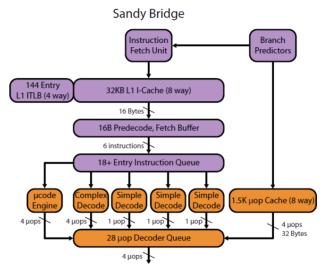
| Demo: | intro/Pipeli | ne Performa | nce Mysterie | <u>es</u> | |
|-------|--------------|-------------|--------------|-----------|--|
| | | | | | |
| | | | | | |
| | | | | | |
| | | | | | |

A Glimpse of a More Modern Processor



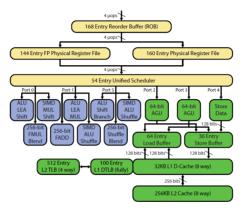
[David Kanter / Realworldtech.com]

A Glimpse of a More Modern Processor: Frontend



[David Kanter / Realworldtech.com]

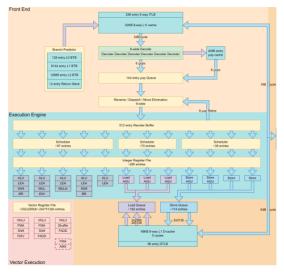
A Glimpse of a More Modern Processor: Backend



- New concept: Instruction-level parallelism ("ILP", "superscalar")
- ▶ Where does the IPC number from earlier come from?

[David Kanter / Realworldtech.com]

A Glimpse of a More Modern Processor: Golden Cove

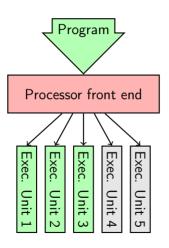


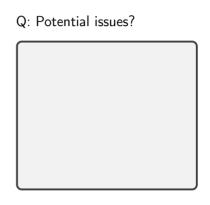
[Wikipedia @]

Demo

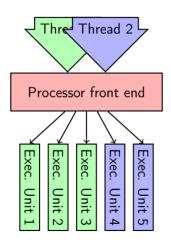
Demo: intro/More Pipeline Mysteries

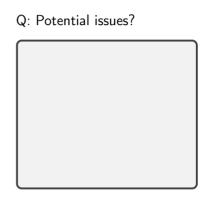
SMT/"Hyperthreading"





SMT/"Hyperthreading"





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More Bad News from Dennard

| Parameter | Factor | |
|-----------------|------------|--|
| Dimension | $1/\kappa$ | |
| Line Resistance | κ | |
| Voltage drop | κ | |
| Response time | 1 | |
| Current density | κ | |

[Dennard et al. '74, via Bohr '07]

- ▶ The above scaling law is for on-chip interconnects.
- ► Current ~ Power *vs.* response time

Getting information from

- processor to memory
- one computer to the next

is

- ▶ slow (in *latency*)
- power-hungry

Somewhere Behind the Interconnect: Memory

Performance characteristics of memory:

- ► Bandwidth
- Latency

Flops are cheap Bandwidth is money Latency is physics — M. Hoemmen

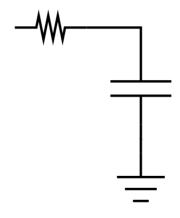
Minor addition (but important for us)?

Latency is Physics: Distance

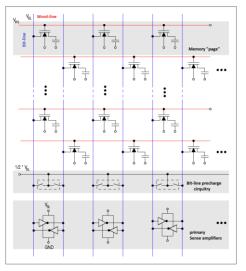


[Wikipedia @]

Latency is Physics: Electrical Model



Latency is Physics: DRAM



[Wikipedia @]

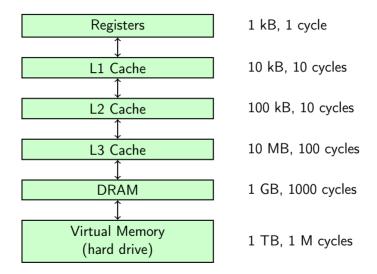
Latency is Physics: Performance Impact?

What is the performance impact of high memory latency?

Idea:

- ▶ Put a look-up table of recently-used data onto the chip.
- ► <u>Cache</u>

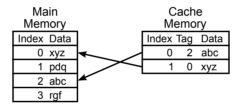
Memory Hierarchy



A Basic Cache

Demands on cache implementation:

- Fast, small, cheap, low power
- Fine-grained
- ► High "hit"-rate (few "misses")



Design Goals: at odds with each other. Why?



[Wikipedia @]

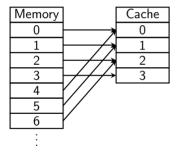
Caches: Engineering Trade-Offs

Engineering Decisions:

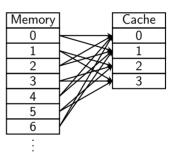
- ► More data per unit of access matching logic
 - → Larger "Cache Lines"
- ► Simpler/less access matching logic
 - ightarrow Less than full "Associativity"
- Eviction strategy
- Size

Associativity

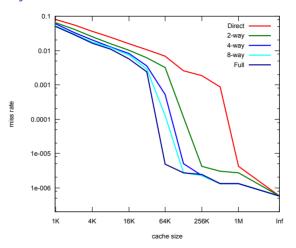
Direct Mapped:



2-way set associative:



Size/Associativity vs Hit Rate



Miss rate versus cache size on the Integer portion of SPEC CPU2000 [Cantin, Hill 2003]

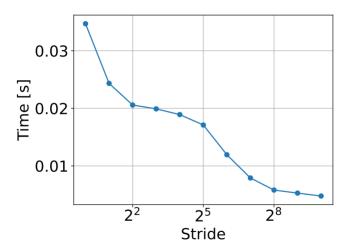
Demo: Learning about Caches

Demo: intro/Cache Organization on Your Machine

Experiments: 1. Strides: Setup

```
int go(unsigned count, unsigned stride)
  const unsigned array size = 64 * 1024 * 1024;
  int *ary = (int *) malloc(sizeof(int) * array size);
  for (unsigned it = 0: it < count: ++it)
    for (unsigned i = 0; i < array size; i += stride)</pre>
      arv[i] *= 17:
  int result = 0:
  for (unsigned i = 0; i < array size; ++i)
      result += arv[i]:
  free (ary);
  return result:
What do you expect? [Ostrovsky '10]
```

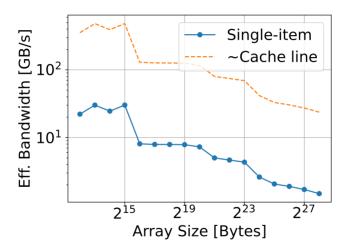
Experiments: 1. Strides: Results



Experiments: 2. Bandwidth: Setup

```
int go(unsigned array size, unsigned steps)
  int *ary = (int *) malloc(sizeof(int) * array size);
  unsigned asm1 = array size - 1;
  for (unsigned i = 0; i < 100*steps;)
   #define ONE ary [(i++*16) \& asm1] ++:
   #define FIVE ONE ONE ONE ONE ONE
   #define TEN FIVE FIVE
   #define FIFTY TEN TEN TEN TEN TEN
   #define HUNDRED FIFTY FIFTY
   HUNDRED
  int result = 0:
  for (unsigned i = 0; i < array size; ++i)
      result += ary[i]:
  free(ary);
  return result;
```

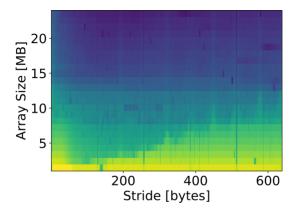
Experiments: 2. Bandwidth: Results



Experiments: 3. A Mystery: Setup

```
int go(unsigned array size, unsigned stride, unsigned steps)
  char *ary = (char *) malloc(sizeof(int) * array size);
  unsigned p = 0:
  for (unsigned i = 0; i < steps; ++i)
    ary[p] ++;
   p += stride:
    if (p >= array size)
     p = 0:
  int result = 0:
  for (unsigned i = 0; i < array size; ++i)
      result += arv[i]:
  free (arv):
  return result:
```

Experiments: 3. A Mystery: Results

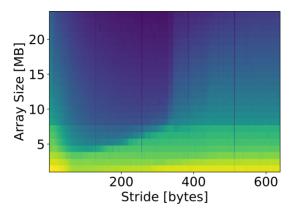


Color represents achieved bandwidth:

Yellow: high

► Blue: low

Experiments: 3. A Mystery: Results on Sandy Bridge



Color represents achieved bandwidth:

Yellow: high

► Blue: low

Thinking about the Memory Hierarchy

- ► What is a working set?
- ► What is data locality of an algorithm?
- ▶ What does this have to with caches?

Case Study: Streaming Workloads

Q: Estimate expected throughput for saxpy on an architecture with caches. What are the right units?

$$z_i = \alpha x_i + y_i \quad (i = 1, \ldots, n)$$

Demo: https://github.com/lcw/stream_ispc

Special Store Instructions

| At least two aspects to keep apart: | |
|---|--|
| | |
| | |
| | |
| What hardware behavior might result from these aspects? | |
| | |
| | |
| | |

- ► Comment on what a compiler can promise on these aspects.
- ► Might these 'flags' apply to loads/prefetches?

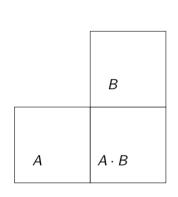
(see also: [McCalpin '18])

Case study: Matrix-Matrix Mult. ('MMM'): Code Structure

- ► How would you structure a high-performance MMM?
- What are sources of concurrency?
- What should you consider your working set?



Case study: Matrix-Matrix Mult. ('MMM'): Code Structure

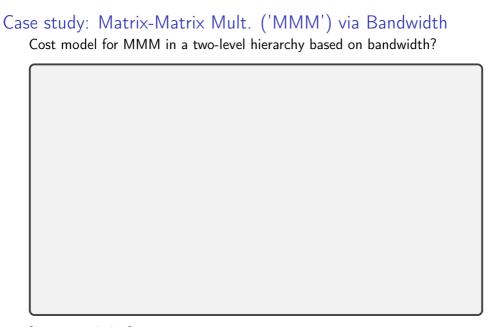


```
for (i)
  for (j)
    for (k)
      c[i,j] += a[i,k]*b[k,j]
After:
for (itile)
  for (itile)
    for (ktile)
      for (iinner)
         for (jinner)
           for (kinner)
             c[itile*NB+iinner,...]
               += ...
```

How many tiles?

Case study: Matrix-Matrix Mult. ('MMM') via Latency Cost model for MMM in a two-level hierarchy based on latency?

[Yotov et al. '07]



[Yotov et al. '07]

Case study: Matrix-Matrix Mult. ('MMM'): Discussion

Discussion: What are the main simplifications in each model?

[Yotov et al. '07]

Q: How can we analyze cache cost of algorithms in general?

Hong/Kung: Red/Blue Pebble Game

Simple means of I/O cost analysis: "Red/blue pebble game"

- ► A way to quantify I/O cost on a DAG (why a DAG?)
- ▶ "Red Hot" pebbles: data that can be computed on
- "Blue Cool" pebbles: data that is stored, but not available for computation without I/O

Game Setup:

Place blue pebbles on inputs

One 'turn':

- ightharpoonup Swap red ightarrow blue or blue ightarrow red
- Place red pebble on successor if all predecessors have red
- Remove any pebble

Note: Can allow "Red/Purple/Blue/Black": more levels [Hong/Kung '81]

Hong/Kung: Red/Blue Pebble Game

| Q: What are the cost metrics in this model? |
|--|
| |
| |
| What does a Hong/Kung lower bound for Matrix-Matrix look like? |
| |
| |

Cache-Oblivious Algorithms

Annoying chore: Have to pick multiple machine-adapted block sizes in cache-adapted algorithms, one for each level in the memory hierarchy, starting with registers.

Idea:

- ▶ Step 1: Express algorithm recursively in divide & conquer manner
- ► Step 2: Pick a strategy to decrease block size Give examples of block size strategies, e.g. for MMM:

Result:

Asymptotically optimal on Hong/Kung metric

Cache-Oblivious Algorithms: Issues

| Observed results? | |
|---|--|
| | |
| What are potential issues on actual hardware? | |
| | |
| | |
| [Votov et al. '07] | |

Recall: Big-O Notation

Classical Analysis of Algorithms (e.g.):

$$Cost(n) = O(n^3).$$

Precise meaning? Anything missing from that statement?

Comment: "Asymptotically Optimal"

Comments on asymptotic statements about cost in relation to high performance?

- No statement about finite n
- ▶ No statement about the constant

Net effect: Having an understanding of asymptotic cost is *necessary*, but *not sufficient* for high performance.

HPC is in the business of minimizing *C* in:

$$Cost(n) \le C \cdot n^3$$
 (for all n)

Alignment

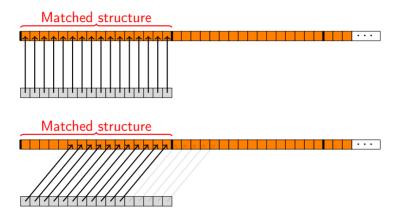
Alignment describes the process of matching the base address of:

- ► Single word: double, float
- SIMD vector
- Larger structure

To machine granularities:

Q: What is the performance impact of misalignment?

Performance Impact of Misalignment



SIMD: Basic Idea

| What's the basic idea behind SIMD? | |
|--|--|
| | |
| | |
| What architectural need does it satisfy? | |
| | |
| | |

Typically characterized by width of data path:

- ► SSE: 128 bit (4 floats, 2 doubles)
- AVX-2: 256 bit (8 floats, 4 doubles)
- ► AVX-512: 512 bit (16 floats, 8 doubles)

SIMD: Architectural Issues

| Realization of inter-lane comm. in SIMD? Find instructions. (Intelntrinsics Guide) |
|--|
| |
| Name tricky/inefficient aspects in terms of expressing SIMD: |
| |
| |

SIMD: Transposes

Why are transposes important? Where do they occur?

Example implementation aspects:

- ► HPTT: [Springer et al. '17]
- ▶ github: springer13/hptt 8x8 transpose microkernel
- ▶ Q: Why 8x8?

Outline

Introduction

Notes

Notes (unfilled, with empty boxes)

Notes (source code on Github)

About This Class

Why Bother with Parallel Computers?

Lowest Accessible Abstraction: Assembly

Architecture of an Execution Pipeline

Architecture of a Memory System

Shared-Memory Multiprocessors

Machine Abstractions

Performance: Expectation, Experiment, Observation

Multiple Cores vs Bandwidth

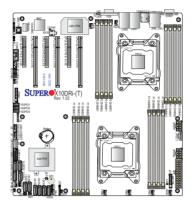
Assume:

- ▶ memory latency of 100 ns
- peak DRAM bandwidth of 100 GB/s (per socket)

How many cache lines should be/are in flight at one time?

[McCalpin '18]

Topology and NUMA



[SuperMicro Inc. '15]

Demo:

- ► Show 1stopo on porter, from hwloc.
- ▶ 1stopo on MI300

Placement and Pinning

| Who decides on what core my code runs? How? |
|---|
| |
| Who decides on what NUMA node memory is allocated? |
| |
| Demo: intro/NUMA and Bandwidths What is the main expense in NUMA? |
| |

Cache Coherence What is cache coherence?

How is cache coherence implemented?

Cache coherence simulation

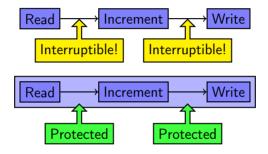
What are the performance impacts?

- ► Demo: intro/Threads vs Cache
- ► Demo: intro/Lock Contention

MESI Sequence to Try

Simplifications in the model?

'Conventional' vs Atomic Memory Update



Outline

Introduction

Machine Abstractions

(

OpenCL/CUDA

Convergence, Differences in Machine Mapping

Lower-Level Abstractions: SPIR-V, PTX

Performance: Expectation, Experiment, Observation

Performance-Oriented Languages and Abstractions

Polyhedral Representation and Transformation

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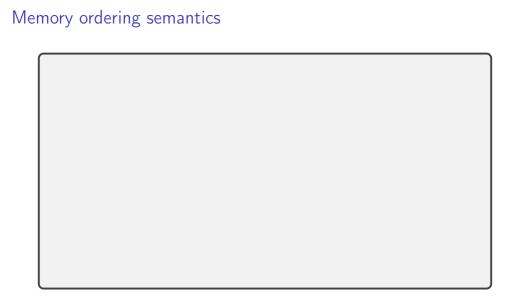
Polyhedral Representation and Transformation

Atomic Operations: Compare-and-Swap

```
#include <stdatomic.h>
Bool atomic compare exchange strong(
       volatile A* obj, C* expected, C desired );
What does volatile mean?
What does this do?
How might you use this to implement atomic FP multiplication?
```

Memory Ordering

| Why is Memory Ordering a Problem? | |
|--|--|
| | |
| | |
| | |
| What's the purpose of different memory orders? | |
| | |
| | |



Example: A Semaphore With Atomics

```
#include <stdatomic.h> // mo ->memory order, a ->atomic
typedef struct { atomic int v;} naive sem t;
void sem down(naive sem t *s)
  while (1) {
    while (a load explicit(\&(s\rightarrow v), mo ) < 1)
        spinloop body();
    int tmp=a fetch add explicit(\&(s\rightarrow v), -1, mo rel);
    if (tmp >= 1)
        break; // we got the lock
    else // undo our attempt
      a fetch add explicit(\&(s\rightarrow v), 1, mo);
void sem up(naive s t *s) {
  a fetch add explicit(\&(s\rightarrow v), 1, mo);
[Cordes '16] — Hardware implementation: how?
```

C: What is 'order'?

C11 Committee Draft, December '10, Sec. 5.1.2.3, "Program execution":

(3) Sequenced before is an asymmetric, transitive, pair-wise relation between evaluations executed by a single thread, which induces a partial order among those evaluations. Given any two evaluations A and B, if A is sequenced before B, then the execution of A shall precede the execution of B. (Conversely, if A is sequenced before B, then B is sequenced after A.) If A is not sequenced before or after B, then A and B are unsequenced. Evaluations A and B are indeterminately sequenced when A is sequenced either before or after B. but it is unspecified which. The presence of a sequence point between the evaluation of expressions A and B implies that every value computation and side effect associated with A is sequenced before every value computation and side effect associated with B. (A summary of the sequence points is given in annex C.)

Q: Where is this definition used (in the standard document)?

C: What is 'order'? (Encore)

C11 Draft, 5.1.2.4 "Multi-threaded executions and data races":

- All modifications to a particular atomic object M occur in some particular total order, called the *modification order* of M.
- ▶ An evaluation A carries a dependency to an evaluation B if . . .
- ▶ An evaluation A is *dependency-ordered* before an evaluation B if. . .
- ▶ An evaluation A *inter-thread happens before* an evaluation B if. . .
- ► An evaluation A happens before an evaluation B if...

Why is this so subtle?

C: How Much Lying is OK?

C11 Committee Draft, December '10, Sec. 5.1.2.3, "Program execution":

- ▶ (1) The semantic descriptions in this International Standard describe the behavior of an abstract machine in which issues of optimization are irrelevant.
- ▶ (2) Accessing a volatile object, modifying an object, modifying a file, or calling a function that does any of those operations are all *side effects*, which are changes in the state of the execution environment. [...]

C: How Much Lying is OK?

- ▶ (4) In the abstract machine, all expressions are evaluated as specified by the semantics. An actual implementation need not evaluate part of an expression if it can deduce that its value is not used and that no needed side effects are produced (including any caused by calling a function or accessing a volatile object).
- ▶ (6) The least requirements on a conforming implementation are:
 - Accesses to volatile objects are evaluated strictly according to the rules of the abstract machine.
 - ▶ At program termination, all data written into files shall be identical to the result that execution of the program according to the abstract semantics would have produced.
 - ▶ The input and output dynamics of interactive devices shall take place as specified in 7.21.3. The intent of these requirements is that unbuffered or line-buffered output appear as soon as possible, to ensure that prompting messages actually appear prior to a program waiting for input.

This is the observable behavior of the program.

Arrays

| Why are arrays the dominant data structure in high-performance code? |
|--|
| |
| |
| |
| Any comments on C's arrays? |
| |
| |

Arrays vs Abstraction

| Arrays-of-Structures or Structures-of-Arrays? Give an example. |
|--|
| |
| |
| |
| |
| |
| Language aspects of the distinction? Salient example? |
| |
| |
| |

C and Multi-Dimensional Arrays: A Saving Grace

```
// YES:
void f(int m, int n, double (*)[m][n]);
// NO:
struct ary {
  int m;
  int n:
  double (*array)[m][n];
};
// YES:
struct ary {
  int m;
  int n;
  double a[];
```

| Name language mechanisms for SIMD: | | | | |
|------------------------------------|--|--|--|--|
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |

Demo: machabstr/Ways to SIMD

Outer-Loop / Inner-Loop Vectorization

| Contrast outer-loop vs inner-loop vectorization. | | | | |
|--|--|--|--|--|
| | | | | |
| | | | | |
| | | | | |
| | | | | |

Side q: Would you consider GPUs outer- or inner-loop-vectorizing?

Alignment: How? The old way: int attribute ((aligned (8))) a int; Difference between these two? int attribute ((aligned (8))) * ptr t 1; int * attribute ((aligned (8))) ptr t 2; The 'new' way (C/C++11): **struct** alignas (64) somestruct t $\{ /* ... */ \}$; struct alignas(alignof(other t)) somestruct t $\{ /* ... */ \}$; struct alignas (std::hardware destructive interference size) somestruct t $\{ /* ... */ \}$;

What is *constructive interference*?

Alignment: Why?

| What is the concrete impact of the constructs on the previous slide? | | | | | |
|--|--|--|--|--|--|
| | | | | | |
| | | | | | |
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| | | | | | |
| | | | | | |

Pointers and Aliasing

Demo: machabstr/Pointer Aliasing

Register Pressure

Demo: machabstr/Register Pressure

| What if the register working set gets larger than the registers can hold? What is the performance impact? |
|---|
| |
| |

Object-Oriented Programming

Demo: machabstr/Object Orientation vs Performance

Being Nice to Your Compiler

Some rules of thumb:

- ► Use indices rather than pointers
- Extract common subexpressions
- ► Make functions static
- ▶ Use const
- ► Avoid store-to-load dependencies

What are the concrete impacts of doing these things?

Outline

Introduction

Machine Abstractions

OpenCL/CUDA

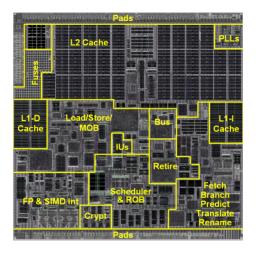
Convergence, Differences in Machine Mapping Lower-Level Abstractions: SPIR-V, PTX

Performance: Expectation, Experiment, Observation

Performance-Oriented Languages and Abstractions

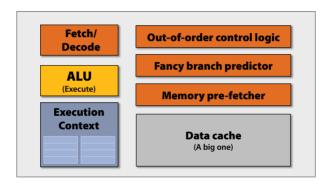
Polyhedral Representation and Transformation

Chip Real Estate

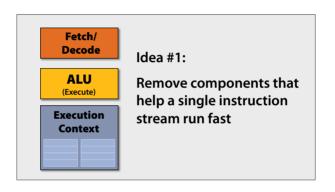


Die floorplan: VIA Isaiah (2008). 65 nm, 4 SP ops at a time, 1 MiB L2.

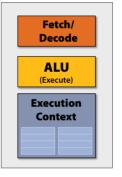
"CPU-style" Cores

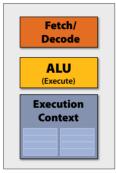


Slimming down

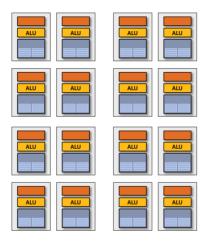


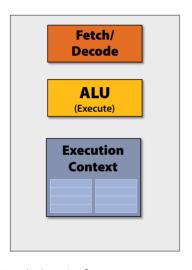
More Space: Double the Number of Cores





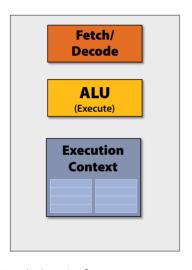
Even more





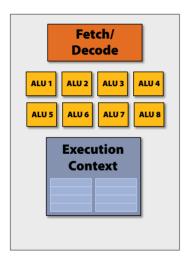
Idea #2: SIMD

[Fatahalian '08]



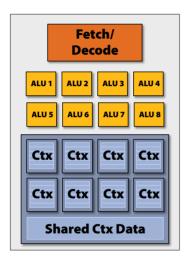
Idea #2: SIMD

[Fatahalian '08]



Idea #2: SIMD

[Fatahalian '08]



Idea #2: SIMD

[Fatahalian '08]

Latency Hiding

- Latency (mem, pipe) hurts non-OOO cores
- ► Do something while waiting

What is the unit in which work gets scheduled on a GPU?



How can we keep busy?



Before:



Scratchpad/L1

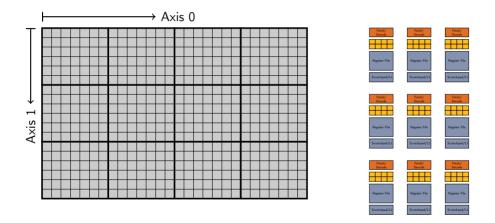




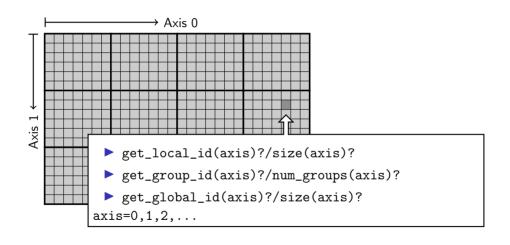
GPUs: Core Architecture Ideas

| Three core ideas: | | | |
|-------------------|--|--|--|
| | | | |
| | | | |
| | | | |
| | | | |
| | | | |

'SIMT'



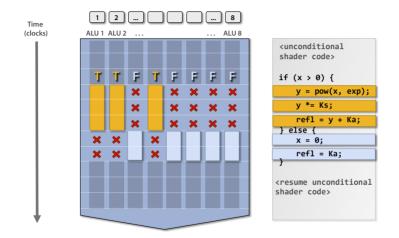
Wrangling the Grid



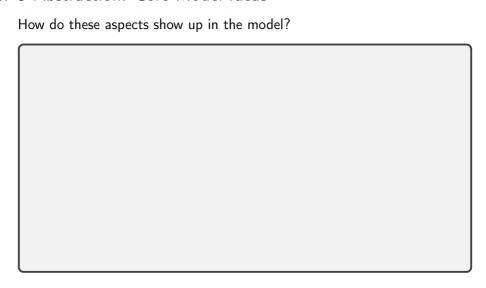
Demo CL code

Demo: machabstr/Hello GPU

'SIMT' and Branches



GPU Abstraction: Core Model Ideas



GPU Address Spaces

| Hardware | CL adjective | OpenCL | CUDA |
|-------------|--------------|-----------|--------------|
| SIMD lane | private | Work Item | Thread |
| SIMD Vector | _ | Subgroup | Warp |
| Core | local | Workgroup | Thread Block |
| Processor | global | NDRange | Grid |

GPU: Communication

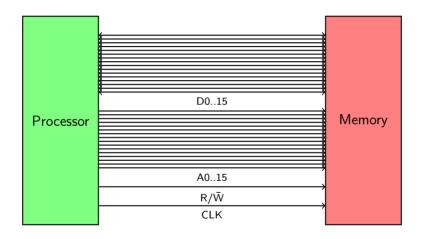
| What forms of communicat | tion exist at each s | scope? |
|-----------------------------|----------------------|--------|
| | | |
| | | |
| Can we just do locking like | we might do on a | CPU? |
| | | |
| | | |
| | | |

GPU Programming Model: Commentary Advantages: Disadvantages:

Performance: Limits to Concurrency

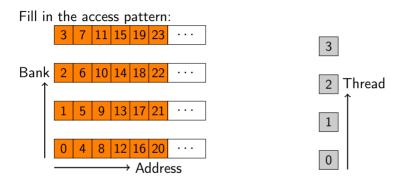
| What limits the amount of concurrency exposed to GPU hardware? | | | | |
|--|--|--|--|--|
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |

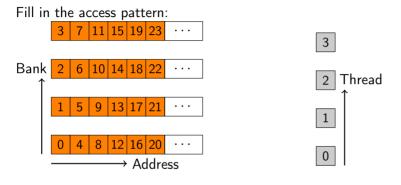
Memory Systems: Recap



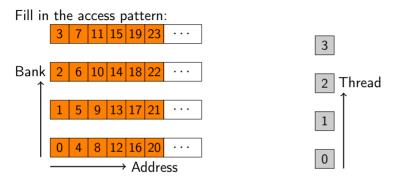
Parallel Memories

| Problem: Memory chips have only one data bus. So how can multiple threads read multiple data items from memory simultaneously? | |
|--|--|
| | |
| Where does banking show up? | |
| | |

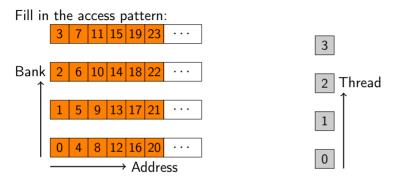




local variable[lid(0)]

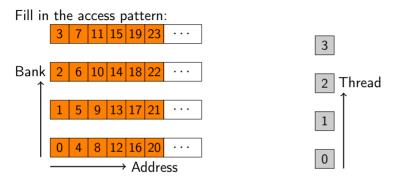


local_variable[BANK_COUNT*lid(0)]



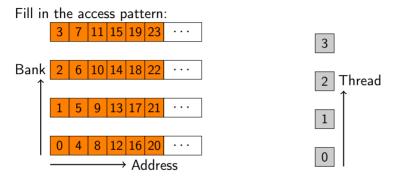
local_variable[(BANK_COUNT+1)*lid(0)]

Memory Banking



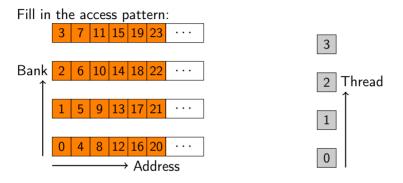
local_variable[ODD_NUMBER*lid(0)]

Memory Banking



local variable[2*lid(0)]

Memory Banking



local_variable[f(gid(0))]

137

Memory Banking: Observations

- Factors of two in the stride: generally bad
- ▶ In a conflict-heavy access pattern, padding can help
 - Usually not a problem since scratchpad is transient by definition

Given that unit strides are beneficial on global memory access, how do you

▶ Word size (bank offset) may be adjustable (Nvidia)

| realize a transpose? | | |
|----------------------|--|--|
| | | |
| | | |
| | | |

Memory Banking: AMD RDNA3 Registers

Manual dual-issue:

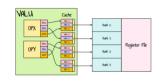
OpCodeX DSTX, SRCXO, SRCX1 :: OpCodeY DSTY, SRCYO, SRCY1

- Insns must be independent
- SRCXO and SRCYO must use different VGPR banks
- Dest VGPRs: one must be even and the other odd

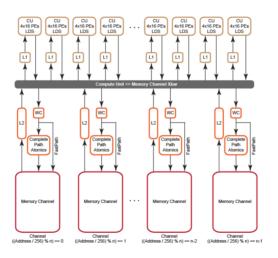
RDNA3 specific:

- There are 4 VGPR banks (indexed by SRC[1:0]), and each bank has a cache.
- Each cache has 3 read ports: one dedicated to SRCO, one dedicated to SRC1 and one for SRC2.
- ▶ A cache can read all 3 of them at once, but it can't read two SRC0's at once (or SRC1/2).

Vince '25



GPU Global Memory System



GCN Optimization Manual, AMD

GPU Global Memory Channel Map: Example

Byte address decomposition:

| | Address | Bank | Chnl | Address | |
|----|---------|------|------|---------|---|
| 31 | Í | ? 11 | 108 | 7 | 0 |

Implications:

- ► Transfers between compute unit and channel have granularity
 - Reasonable guess: warp/wavefront size × 32bits
 - ► Should strive for good utilization ('Coalescing')
- ► Channel count often *not* a power of two -> complex mapping
 - Channel conflicts possible
- Also banked
 - Bank conflicts also possible

GPU Global Memory: Performance Observations

Key quantities to observe for GPU global memory access:

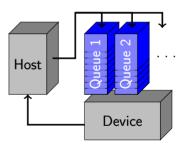
| ^ | .1 | | | 2 | |
|---|----|--|--|---|--|

Are there any guaranteed-good memory access patterns?

- ▶ Need to consider access pattern across entire device
- ► GPU caches: Use for spatial, not for temporal locality
- ► Switch available: L1/Scratchpad partitioning
 - Settable on a per-kernel basis
- ► Since GPUs have meaningful caches at this point: Be aware of cache annotations (see later)

Host-Device Concurrency

- Host and Device run asynchronously
- Host submits to queue:
 - Computations
 - Memory Transfers
 - Sync primitives
 - ..
 - ▶ Batches of these
 - Mutable batches of these
 - Nvidia: "CUDA Graphs"
 - OpenCL: "Command buffers"
- Host can wait for:
 - drained queue
 - ► Individual "events"
- Profiling



Timing GPU Work

| low do you find the exe | cution time o | of a GPU ke | rnel? | |
|-------------------------|---------------|-------------|-------|--|
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| | | | | |
| low do you do this asyı | nchronously? | | | |
| | | | | |
| | | | | |

Host-Device Data Exchange

Sad fact: Must get data onto device to compute

- ► Transfers can be a bottleneck
- ▶ If possible, overlap with computation
- Pageable memory incurs difficulty in GPU-host transfers, often entails (another!) CPU side copy
- "Pinned memory": unpageable, avoids copy
 - Various system-defined ways of allocating pinned memory

"Unified memory" (CUDA)/"Shared Virtual Memory" (OpenCL):

- ► GPU directly accesses host memory
- ► Main distinction: Coherence
 - "Coarse grain": Per-buffer fences
 - "Fine grain buffer": Byte-for-byte coherent (device mem)
 - "Fine grain system": Byte-for-byte coherent (anywhere)

| Bandwidth on device (A100 PCIe) | : | |
|---------------------------------|---|--|
| | | |
| Flop throughput? (A100 PCIe) | | |
| | | |
| Kernel launch overhead? | | |

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Convergence, Differences in Machine Mapping

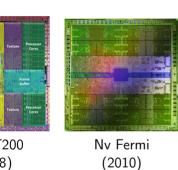
Lower-Level Abstractions: SPIR-V, PTX

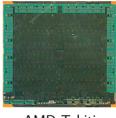
Performance: Expectation, Experiment, Observation

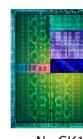
Performance-Oriented Languages and Abstractions

Polyhedral Representation and Transformation

Die Shot Gallery (old)





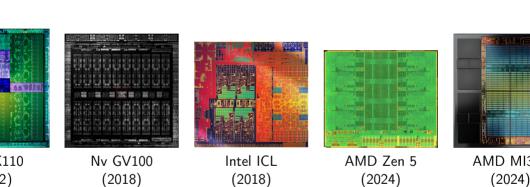


Intel IVB (2012)

AMD Tahiti (2012)

Nv GK1 (2012)

Die Shot Gallery (new)



Trends in Processor Architecture

| What can we expect from future processor architectures? | | | | |
|---|--|--|--|--|
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Common Challenges

| What are the common challenges encountered by both CPUs and GPUs? |
|---|
| |
| |
| |

Goal: Try to see CPUs and GPUs as points in a design space 'continuum' rather than entirely different things.

Outline

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OpenCL/CUDA

Convergence, Differences in Machine Mapping

Lower-Level Abstractions: SPIR-V, PTX

Performance: Expectation, Experiment, Observation

Performance-Oriented Languages and Abstractions

Polyhedral Representation and Transformation

PTX: Demo

Demo: machabstr/PTX and SASS Nvidia PTX manual

PTX: Cache Annotations

Loads:

- .ca Cache at all levels-likely to be accessed again
- .cg Cache at global level (cache in L2 and below and not L1)
- .cs Cache streaming-likely to be accessed once
- .lu Last use
- .cv Consider cached system memory lines stale-fetch again

Stores:

- .wb Cache write-back all coherent levels
- .cg Cache at global level (cache in L2 and below and not L1)
- .cs Cache streaming-likely to be accessed once
- .wt Cache write-through (to system memory)

Lost/hidden at the C level!

SPIR-V

Currently: C (OpenCL C, GLSL, HLSL) used as intermediate representations to feed GPUs.

Downsides:

- ► Compiler heuristics may be focused on human-written code
- Parsing overhead (preprocessor!)
- ► C semantics may not match (too high-level)

SPIR-V:

- Goal: Common intermediate representation ("IR") for all GPU-facing code (Vulkan, OpenCL)
- "Extended Instruction Sets":
 - ► General compute (OpenCL/CUDA) needs: pointers, special functions
- ▶ Different from "SPIR" (tweaked LLVM IR)

SPIR-V Example

```
%2 = OpTypeVoid
          %3 = OpTypeFunction %2
                                                      : void ()
                                                      ; 32-bit float
         %6 = OpTypeFloat 32
         %7 = OpTypeVector %6 4
                                                      : vec4
         %8 = OpTypePointer Function %7
                                                       : function-local vec4*
         %10 = OpConstant %6 1
         %11 = OpConstant %6 2
         %12 = OpConstantComposite %7 %10 %10 %11 %10; vec4(1.0, 1.0, 2.0, 1.0)
         %13 = OpTvpeInt 32 0
                                                       ; 32-bit int, sign-less
         %14 = OpConstant %13 5
         %15 = OpTypeArray %7 %14
Γ...1
         %34 = OpLoad %7 %33
         %38 = OpAccessChain %37 %20 %35 %21 %36
                                                      : s.v[2]
         %39 = OpLoad %7 %38
         %40 = OpFAdd %7 %34 %39
               OpStore %31 %40
              OpBranch %29
         %41 = OpLabel
                                                       ; else
         %43 = OpLoad %7 %42
         %44 = OpExtInst %7 %1 Sqrt %43
                                                       ; extended instruction sqrt
         %45 = OpLoad %7 %9
         %46 = OpFMul %7 %44 %45
```

OpStore %31 %46

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Profiling and Observable Quantities
Practical Tools: perf. toploy, likewid

Practical Tools: perf, toplev, likwid

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Qualifying Performance

- ▶ What is *good* performance?
- ► Is speed-up (e.g. GPU vs CPU? C vs Matlab?) a meaningful way to assess performance?
- ▶ How else could one *form an understanding* of performance?

Hager et al. '17 Hockney et al. '89

A Story of Bottlenecks

| 1 | m | 1 | gi | n | Δ | • |
|---|---|---|-----|----|---|---|
| | | а | ຮຸເ | 11 | C | |

- ► A bank with a few service desks
- ► A revolving door at the entrance

| What | situations c | an arise at | steady-state | ? | | |
|-------|--------------|-------------|---------------|--------------|-----------------|-----|
| | | | | | | |
| \ | | | | | C.1. | |
| vvnat | numbers do | we need to | o characteriz | e performano | e of this syste | m (|
| | | | | | | |
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A Story of Bottlenecks (cont'd)

- ► P_{peak}: [task/sec] Peak throughput of the service desks
- ► 1: [tasks/customer] Intensity
- b: [customers/sec] Throughput of the revolving door

What is the aggregate throughput?

Hager et al. '17

Application in Computation

| ranslate the bank analogy to computers: | |
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| /hich parts of this are task-dependent? | |
| | |
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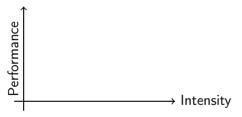
A Graphical Representation: 'Roofline'

Plot (often log-log, but not necessarily):

- X-Axis: Intensity
- Y-Axis: Performance

What does our inequality correspond to graphically?

$$P \leq \min(P_{\mathsf{peak}}, I \cdot b)$$



What does the shaded area mean?

Example: Vector Addition

```
double r, s, a[N];
for (i=0; i<N; ++i)
  a[i] = r + s * a[i];}</pre>
```

Find the parameters and make a prediction.



rformance

Refining the Model

- ▶ P_{max} : Applicable peak performance of a loop, assuming that data comes from the fastest data path (this is not necessarily P_{peak})
- Computational intensity ("work" per byte transferred) over the slowest data path utilized
- b: Applicable peak bandwidth of the slowest data path utilized

Hager et al. '17

Calibrating the Model: Bandwidth

```
Typically done with the STREAM benchmark.
Four parts: Copy, Scale, Add, Triad a[i] = b[i] + s\cdot c[i]
Do the four measurements matter?
Any pitfalls?
McCalpin: STREAM
```

Calibrating the Model: Peak Throughput

Practical Tool: IACA

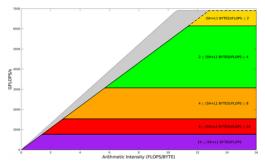
Question: Where to obtain an estimate of P_{max} ?

Demo: perf/Forming Architectural Performance Expectations

Questions:

▶ What does IACA do about memory access? / the memory hierarchy?

An Example: Exploring Titan V Limits



- ▶ Memory bandwidth: 652 GB/s theoretical, 540 GB/s achievable
- Scratchpad / L1 throughput: 80 (cores) x 32 (simd width) x 4 (word bytes) x 1.2 (base clock) ~= 12.288 TB/s
- ► Theoretical peak flops of 6.9 TFLOPS/s [Wikipedia]

Warburton '18

Rooflines: Assumptions

| What assumptions are built into the roofline model? | | | | | |
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Important to remember:

- It is what you make of it—the better your calibration, the more info you get
- But: Calibrating on experimental data loses predictive power (e.g. SPMV)

Modeling Parallel Speedup: A 'Universal' Scaling Law

Develop a model of throughput X(N) for a given load N, assuming execution resources scale with N.

[Gunther '93]

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Combining Multiple Measurements

How can one combine multiple performance measurements? (e.g. "average speedup"?)

Example: Which computer should you buy?

| Execution time [s] | Computer A | Computer B | Computer C |
|--------------------|------------|------------|------------|
| Program 1 | 1 | 10 | 20 |
| Program 2 | 1000 | 100 | 20 |

Combining Multiple Measurements: Observations

| | Computer A | Computer B | Computer C | |
|-----------------|------------|------------|------------|--|
| Arithmetic mean | 500.5 | 55 | 20 | |
| Geometric mean | 31.622 | 31.622 | 20 | |
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Timing Experiments: Pitfalls

| Vhat are potential issues in timing experiments? (What can you do about hem?) |
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Timing Experiments: Pitfalls (part 2) What are potential issues in timing experiments? (What can you do about them?)

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Profiling: Basic Approaches

Measurement of "quantities" relating to performance

- ► Exact: Through binary instrumentation (valgrind/Intel Pin/...)
- ▶ Sampling: At *some* interval, examine the program state

We will focus on profiling by sampling.

Big questions:

- ► What to measure?
- At what intervals?

Defining Intervals: Performance Counters

A *performance counter* is a counter that increments every time a given event occurs.

What events?

- ► Demo: perf/Using Performance Counters
- ► see also Intel SDM, Volume 3

Interaction with performance counters:

- Read repeatedly from user code
- Interrupt program execution when a threshold is reached
- Limited resource!
 - Only a few available: 4-8 per core
 - Each can be configured to count one type of event
 - Idea: Alternate counter programming at some rate (requires steady-state execution!)

Profiling: What to Measure

- ► Raw counts are hard to interpret
- ▶ Often much more helpful to look at *ratios* of counts per core/subroutine/loop/...

What ratios should one look at?

Demo: perf/Using Performance Counters

Profiling: Useful Ratios

Basic examples:

- ► (Events in Routine 1)/(Events in Routine 2)
- ► (Events in Line 1)/(Events in Line 2)
- ► (Count of Event 1 in X)/(Count of Event 2 in X)

| Architectural examples: | | | | | |
|-------------------------|--|--|--|--|--|
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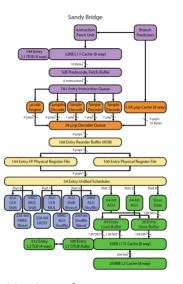
Issue with 'instructions' as a metric?

"Top-Down" Performance Analysis

Idea: Account for useful work per available issue slot What is an issue slot?

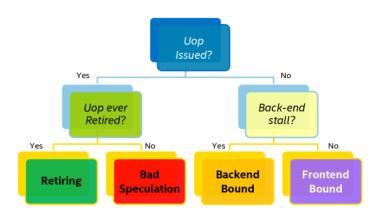
[Yasin '14]

Issue Slots: Recap



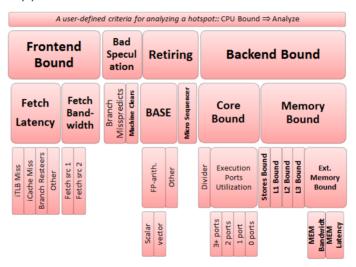
[David Kanter / Realworldtech.com]

What can happen to an issue slot: at a high level?



[Yasin '14]

What can happen to an issue slot: in detail?



[Yasin '14]

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Demo: Performance Counters

Show the rest of:

Demo: perf/Using Performance Counters

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Expression Trees and Term Rewriting

Demos:

- ► Demo: lang/01 Expression Trees
- ► Demo: lang/02 Traversing Trees
- ► Demo: lang/03 Defining Custom Node Types
- ► Demo: lang/04 Common Operations

How do expression trees come to be? (not our problem here)

Embedded languages

| Main challenge: Obtaining a syntax tree. Appro | paches? |
|--|---------|
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Macros: Goals and Approaches

| Vhat is a macro? | |
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| Vhat data do macro systems operate on? | |
| | |
| | |

Macros: Textual and Syntactic, Hygiene

```
Macros: What can go wrong if you're not careful?
#define INCI(i) do { int a=0; ++i; } while(0)
int main(void)
    int a = 4. b = 8:
     INCI(a):
     INCI(b):
     printf("a_is_now_%d,_b_is_now_%d\n", a, b);
     return 0:
How can the problem above be avoided?
```

Towards Execution

Demo: lang/06 Towards Execution

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Reduction

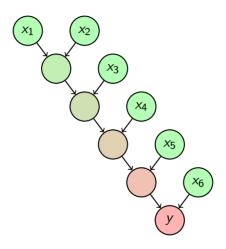
$$y = f(\cdots f(f(x_1, x_2), x_3), \ldots, x_N)$$

where N is the input size.

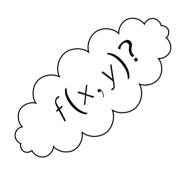
Also known as

- ► Lisp/Python function reduce (Scheme: fold)
- ► C++ STL std::accumulate

Reduction: Graph



Approach to Reduction



Can we do better?

"Tree" very imbalanced. What property of f would allow 'rebalancing'?

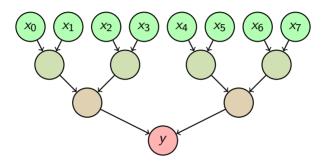
$$f(f(x,y),z)=f(x,f(y,z))$$

Looks less improbable if we let $x \circ y = f(x, y)$:

$$x\circ (y\circ z))=(x\circ y)\circ z$$

Has a very familiar name: Associativity

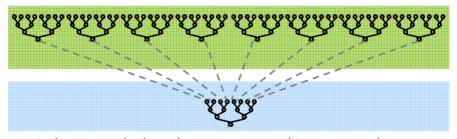
Reduction: A Better Graph



Processor allocation?

Mapping Reduction to SIMD/GPU

- ▶ Obvious: Want to use tree-based approach.
- ▶ Problem: Two scales, Work group and Grid
 - to occupy both to make good use of the machine.
- In particular, need synchronization after each tree stage.
- ► Solution: Use a two-scale algorithm.



In particular: Use multiple grid invocations to achieve inter-workgroup synchronization.

Map-Reduce

But no. Not even close.

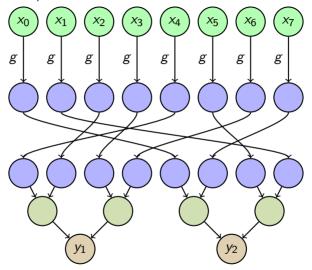
Sounds like this:

$$y = f(\cdots f(f(g(x_1), g(x_2)), g(x_3)), \ldots, g(x_N))$$

where N is the input size.

- Lisp naming, again
- Mild generalization of reduction

Map-Reduce: Graph



Scan

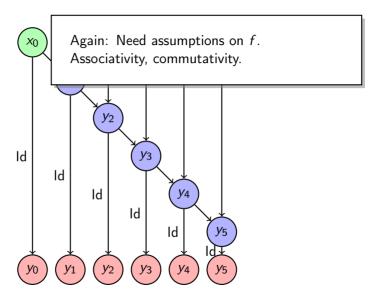
$$y_1 = x_1$$

 $y_2 = f(y_1, x_2)$
 $\vdots = \vdots$
 $y_N = f(y_{N-1}, x_N)$

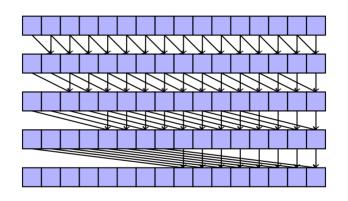
where N is the input size. (Think: N large, f(x,y) = x + y)

- Prefix Sum/Cumulative Sum
- ► Abstract view of: loop-carried dependence
- ► Also possible: Segmented Scan

Scan: Graph



Scan: Implementation



Work-efficient?

Scan: Implementation II

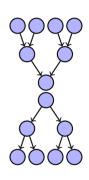
Two sweeps: Upward, downward, both tree-shape

On upward sweep:

- ► Get values L and R from left and right child
- ► Save L in local variable Mine
- Compute Tmp = L + R and pass to parent

On downward sweep:

- ► Get value Tmp from parent
- ► Send Tmp to left child
- Sent Tmp+Mine to right child

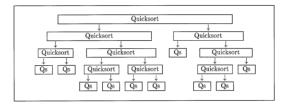


Scan: Examples

| Name examples of Prefix Sums/Scans: | | | | |
|-------------------------------------|--|--|--|--|
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Data-parallel language: Goals

Goal: Design a full data-parallel programming language Example: What should the (asymptotic) execution time for Quicksort be?



| Question: | : What parallel primitive could be used to realize this? | |
|-----------|--|--|
| | | |
| | | |

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NESL Example: String Search

```
teststr = "string strap asop string" : [char]
>>> candidates = [0:#teststr-5]:
candidates = [0, 1, 2, 3, .... : [int]]
>>> {a == 's: a in teststr -> candidates}:
it = [T, F, F, F, F, F, T, F, F, \dots] : [bool]
>>> candidates = {c in candidates:
          a in teststr -> candidates | a == 's}:
candidates = [0, 7, 13, 20, 24] : [int]
>>> candidates = {c in candidates:
          a in teststr -> {candidates+1:candidates}
          l a == 't}:
```

- ► Work and depth of this example?
- ▶ NESL specifies work and depth for its constructs
- ► How can scans be used to realize this?

Blelloch '95

Array Languages

Idea:

- Operate on entire array at once
- ► Inherently data-parallel

Examples:

- ► APL, numpy
- ► Tensorflow (talk on Friday), Pytorch

Important axes of distinction:

- Lazy or eager
- ▶ Imperative (with in-place modification) or pure/functional

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Polyhedral Representation and Transformation Polyhedral Model: What?

Basic Object: Presburger Set

Think of the problem statement here as representing an arbitrary-size (e.g.: dependency) graph.

Presburger sets correspond to a subset of predicate logic acting on tuples of integers.

Important: Think of this as a mathematical tool that can be used in many settings.

Basic Object: Presburger Set

Terms:

- ► Variables, Integer Constants
- **▶** +, -
- $\triangleright \lfloor \cdot/d \rfloor$

Predicates:

- ightharpoonup (Term) \leq (Term)
- ▶ $(Pred) \land (Pred), (Pred) \lor (Pred), \neg (Pred)$
- $ightharpoonup \exists v : (\mathsf{Pred})(v)$

Sets: integer tuples for which a predicate is true Verdoolaege '13

Presburger Sets: Reasoning

| What's "missing"? Why? | |
|------------------------------------|--|
| | |
| | |
| Why is this called 'quasi-affine'? | |
| | |
| | |

Presburger Sets: Reasoning

| What do the resulting sets have to do with polyhedra? When are they convex? |
|---|
| |
| Why polyhedra? Why not just rectangles? |
| |
| |

Demo: Constructing and Operating on Presburger Sets

Demo: lang/Operating on Presburger Sets

Making Use of Presburger Sets

- ► Loop Domains
- Array Access Relations (e.g. write, read: per statement)
- Schedules, with "lexicographic time"
- Dependency graphs
- ► (E.g. cache) interference graphs
- Q: Specify domain and range for the relations above.

Example: Dependency Graph

Given:

- \blacktriangleright Write access relation W: Loop domain \rightarrow array indices
- Read access relation R
- Schedule S for statement S_i : Loop domain $D \to \text{lex}$. time of statement instance
- ► Relation <: Lexicographic 'before'

Find the dependency graph:

Verdoolaege '13

Example: Last Instance

Given:

- ightharpoonup Write access relation W: Loop domain ightharpoonup array indices
- Read access relation R
- ▶ Schedule *S* for statement S_i : Loop domain $D \rightarrow \text{lex}$. time of statement instance
- ► Relation ≺: Lexicographic 'before'

Find the statement instances accessing array element:

Find the *last* statement instance accessing array element:

Verdoolaege '13

Primitive Transformations (I)

| Source Code | Partition | Transformed Code |
|---|-----------------------------------|---|
| for (i=1; i<=N; i++) Y[i] = Z[i]; /*s1*/ for (j=1; j<=N; j++) X[j] = Y[j]; /*s2*/ | Fusion $s_1: p = i$ $s_2: p = j$ | for (p=1; p<=N; p++){ Y[p] = Z[p]; X[p] = Y[p]; } |
| for (p=1; p<=N; p++){ Y[p] = Z[p]; X[p] = Y[p]; } | Fission $s_1: i = p$ $s_2: j = p$ | for (i=1; i<=N; i++) Y[i] = Z[i]; /*s1*/ for (j=1; j<=N; j++) X[j] = Y[j]; /*s2*/ |

Primitive Transformations (II)

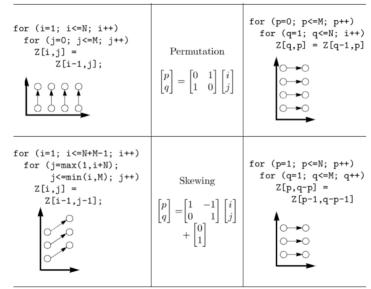
```
if (N>=1) X[1]=Y[0];
                                          for (p=1; p<=N-1; p++){}
for (i=1; i<=N; i++) {
  Y[i] = Z[i]; /*s1*/
                                            Y[p]=Z[p];
                                            X[p+1]=Y[p];
  X[i] = Y[i-1]; /*s2*/
                             Re-indexing
                              s_1 : p = i
                                          if (N>=1) Y[N]=Z[N];
                            s_2: p = i - 1
                                          for (p=1; p<=2*N; p++){}
for (i=1; i<=N; i++)
                                            if (p \mod 2 == 0)
  Y[2*i] = Z[2*i]; /*s1*/
                                              Y[p] = Z[p];
for (j=1; j \le 2N; j++)
                               Scaling
                                            X[p] = Y[p];
  X[j]=Y[j];
                  /*s2*/
                             s_1: p = 2 * i
                             (s_2: p = j)
```

Primitive Transformations (III)

| | | Transformed Code |
|---|--|---|
| for (i=0; i>=N; i++) Y[N-i] = Z[i]; /*s1*/ for (j=0; j<=N; j++) X[j] = Y[j]; /*s2*/ | Reversal $s_1: p = N - i$ $(s_2: p = j)$ | for (p=0; p<=N; p++){ Y[p] = Z[N-p]; X[p] = Y[p]; } |

[Aho/Ullman/Sethi '07]

Primitive Transformations (IV)



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Example: Last Instance

Given:

► Dependency relation *D*

Check whether a transformed schedule S' is valid:

A peek under the hood: Fourier-Motzkin Elimination

INPUT: A polyhedron S with variables $x1, \ldots, x_n$ OUTPUT: $x1, \ldots, x_{n-1}$

- ▶ Let C be all the constraints in S involving x_n .
- For every pair of a lower and an upper bound on x_m in C:

$$L \leq c_1 x_n, \\ \leq c_2 x_n \leq U,$$

create the new constraint $c_2L \leq c_1U$.

- ▶ Divide by the GCD of c_1 , c_2 if applicable.
- ▶ If the new constraint is not satisfiable, *S* was empty.
- ▶ Let $S' = S \setminus C \cup \bigcup_{L,U} \{c_2L \leq c_1U\}$.

[Aho/Ullman/Sethi '07]

Q: How can this help implement an emptiness check?